

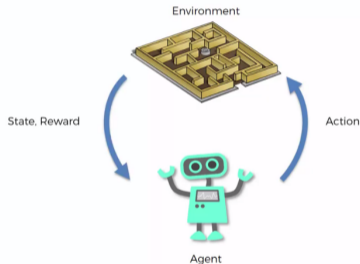
A Simple Reward-Free Approach to Constrained Reinforcement Learning

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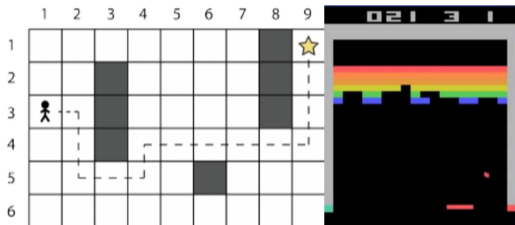
Agent interactively takes some action in the Environment and receives some **scalar reward** for the action taken.



Goal: find policy that maximizes the cumulative **scalar reward**

Reward Models Desired Behavior

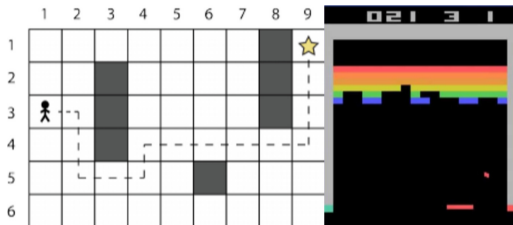
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Desired behavior is simple

- Agent needs to reach the “goal” as “quickly” as possible (e.g., gridworld)

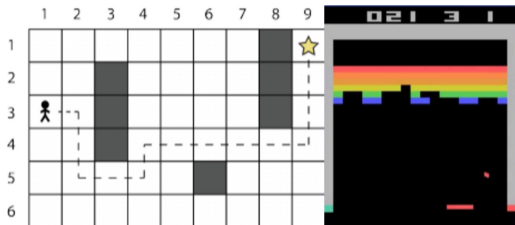
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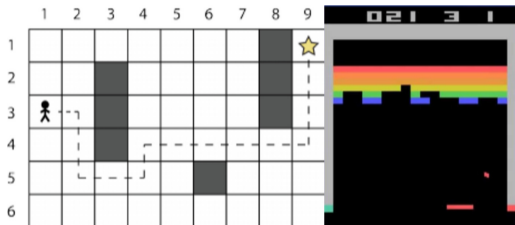
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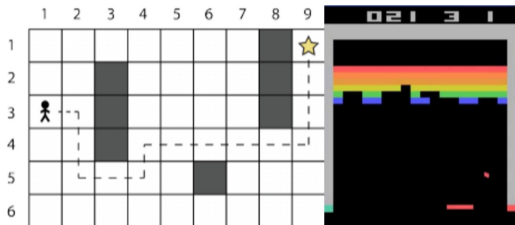
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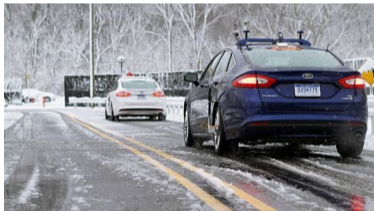
Strategy: applying standard RL using positive and negative scalar rewards.

Complex Desired Behavior

Desired behavior is **complex** and it consists of many **subgoals** and **restrictions**

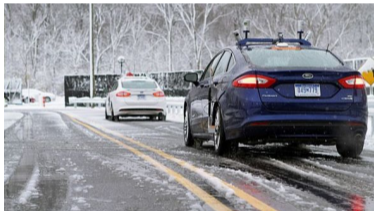
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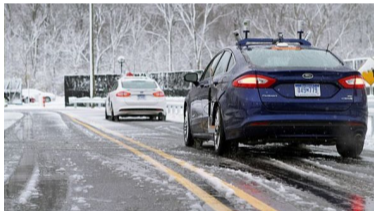
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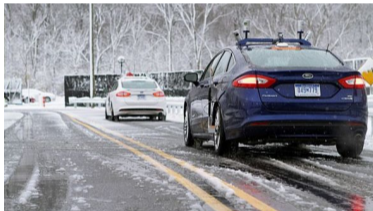
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- Robot should **not only fulfill its task**, but should also control its **wear and tear** (e.g., limiting torque on its motors)

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- ...

One Approach: applying standard RL

- Boiling down learning goal into a **single scalar** is challenging
- Agent might maximize the reward without satisfying our desired behavior
- Gets harder as desired behavior gets more complex

Better Approach: Constraint-Based RL

In many settings, it's more natural and easier to express some behaviors by **constraints**.

Framework that bridges **Reward-free RL** and **Constrained RL**

- Direct translation of any progress in **Reward-free RL** to **Constrained RL**
- While being **modular**, provides **sharp sample complexity** for the **tabular setting**
- Providing **first** sample complexity results for **linear setting**

Model: Episodic VMDP

Episodic **vector-valued** Markov Decision Process (VMDP) $\mathcal{M} = (\mathcal{S}, \mathcal{A}, H, \mathbb{P}, \mathbf{r})$ Same as MDP model except \mathbf{r} is **d -dimensional**

- **vector-valued** value function \mathbf{V}_h^π and \mathbf{Q}_h^π

Scalarized MDP: For any $\boldsymbol{\theta} \in \mathbb{R}^d$, define $\mathcal{M}_\theta = (\mathcal{S}, \mathcal{A}, H, \mathbb{P}, r_\theta)$ where $r_\theta = \langle \boldsymbol{\theta}, \mathbf{r} \rangle$

- scalarized value functions $V_h^\pi(\cdot; \boldsymbol{\theta})$ and $Q^\pi(\cdot, \cdot; \boldsymbol{\theta})$
- optimal value function $V_h^*(\cdot; \boldsymbol{\theta})$ and $Q_h^*(\cdot, \cdot; \boldsymbol{\theta})$

Learning Objective(s)

Assume \mathcal{C} is a convex and compact set in \mathbb{R}^d .

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Task 3: Constrained RL

Assume utility function

$$u = \{u_h : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}\}_{h=1}^H$$

$$\max_{\pi} \mathbb{E}_{\pi} \left[\sum_h u_h(s_h, a_h) \right]$$

$$\text{s.t. } \mathbf{V}_1^{\pi}(s_1) \in \mathcal{C}$$

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Assume \mathcal{C} is a convex and compact set in \mathbb{R}^d .

Task 2: Approachability

$$\min_{\pi} \text{dist}\left(\mathbf{V}_1^{\pi}(s_1), \mathcal{C}\right)$$

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Learning Objective(s)

Assume \mathcal{C} is a convex and compact set in \mathbb{R}^d .

Task 1: Reward-free

After exploration phase,

$\{r_h(s_h^k, a_h^k)\}_{(k,h) \in [K] \times [H]}$ are revealed

for any $\theta \in \mathbb{R}^d$, algorithm should output the (near-)optimal policy π_θ that maximizes $V_1^{\pi_\theta}(s_1; \theta)$

Task 2: Approachability

$$\min_{\pi} \text{dist}\left(\mathbf{V}_1^{\pi}(s_1), \mathcal{C}\right)$$

Task 3: Constrained RL

Assume utility function

$$u = \{u_h : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}\}_{h=1}^H$$

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Reductions

Task 1: Reward-free

**Task 2:
Approachability**

**Task 3: Constrained
RL**

Reductions

Task 1: Reward-free

It's easy to show that

Task 2:
Approachability



Task 3: Constrained
RL

$$\text{Sample Complexity of Task 3} \leq \tilde{O}\left(\text{Sample Complexity of Task 2} + \underbrace{H^2 \log[d]/\epsilon^2}_{\text{usually lower order term}} \right)$$

Reductions



We design a **Meta Algorithm** that satisfies

Main Result

$$\text{Sample Complexity of Task 2} \leq \tilde{O}\left(\text{Sample Complexity of Task 1} + \underbrace{H^2 \log[d]/\epsilon^2}_{\text{usually lower order term}} \right)$$

Sample Complexity Guarantees

	Algorithm	T1: Reward-free	T2: Approachability	T3: CMDP
Tabular	[WBY20]	$\tilde{O}(\min\{d, S\}H^4SA/\epsilon^2)$	-	-
	[BDL ⁺ 20]	-	-	$\tilde{O}(d^2H^3S^2A/\epsilon^2)$
	[YTZS21]	-	$\tilde{O}(\min\{d, S\}H^3SA/\epsilon^2)$	$\tilde{O}(\min\{d, S\}H^3SA/\epsilon^2)$
	This work	$\tilde{O}(\min\{d, S\}H^4SA/\epsilon^2)$	$\tilde{O}(\min\{d, S\}H^4SA/\epsilon^2)$	$\tilde{O}(\min\{d, S\}H^4SA/\epsilon^2)$
Linear	This work	$\tilde{O}(d_{\text{lin}}^3H^6/\epsilon^2)$	$\tilde{O}(d_{\text{lin}}^3H^6/\epsilon^2)$	$\tilde{O}(d_{\text{lin}}^3H^6/\epsilon^2)$

References

- [BDL⁺20] Kianté Brantley, Miro Dudik, Thodoris Lykouris, Sobhan Miryoosefi, Max Simchowitz, Aleksandrs Slivkins, and Wen Sun. Constrained episodic reinforcement learning in concave-convex and knapsack settings. In *Advances in Neural Information Processing Systems*, volume 33, pages 16315–16326. Curran Associates, Inc., 2020.
- [WBY20] Jingfeng Wu, Vladimir Braverman, and Lin F Yang. Accommodating picky customers: Regret bound and exploration complexity for multi-objective reinforcement learning. *arXiv preprint arXiv:2011.13034*, 2020.
- [YTZS21] Tiancheng Yu, Yi Tian, Jingzhao Zhang, and Suvrit Sra. Provably efficient algorithms for multi-objective competitive rl. *arXiv preprint arXiv:2102.03192*, 2021.